



VARIATION OF THE MEASUREMENT UNCERTAINTY WITH MEASURAND LEVEL

Eskil Sahlin

Eurachem Workshop 25-26 Oct 2022

Research Institutes of Sweden

1

Top down evaluation of measurement uncertainty - Measurand level (often concentration) dependence

- Based on different types of precision and bias
- Often calculated from samples at different concentration levels
- Important to know the concentration dependence of the measurement uncertainty

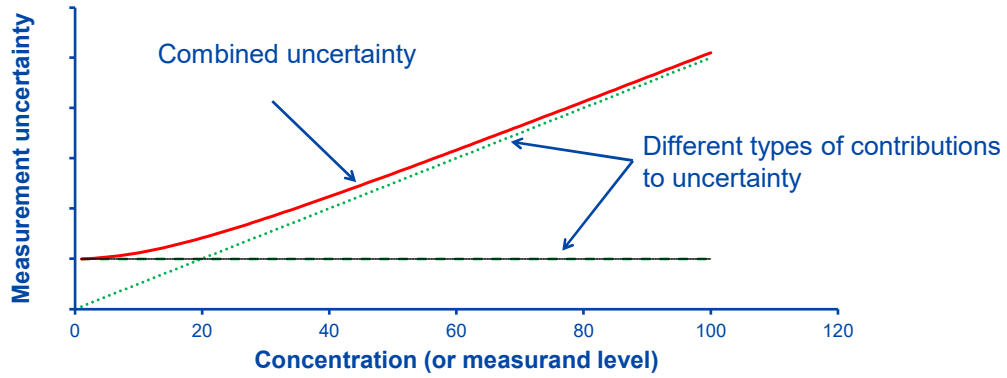
Eurachem workshop 2022



2

2

Typical dependence of concentration (measurand level) on measurement uncertainty for many instrumental techniques



Eurachem workshop 2022

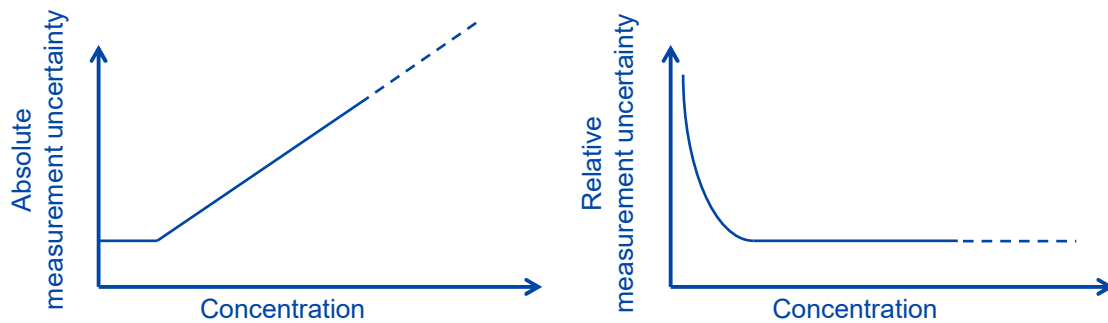


3

3

Typical dependence of concentration (measurand level) on measurement uncertainty for many instrumental techniques

Simplification:



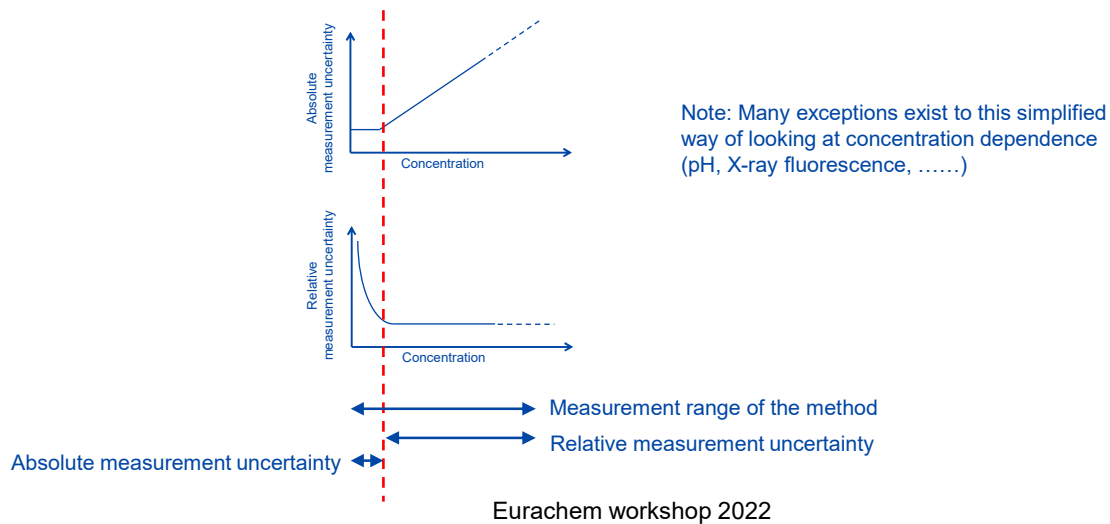
Eurachem workshop 2022



4

4

Typical dependence of concentration (measurand level) on measurement uncertainty for many instrumental techniques



5

5

To reality – What is the concentration dependence for your method?

To study this, ideally large amount of data is needed that are rarely available

Way of studying dependence of concentration (measurand level) on measurement uncertainty

Precision:

- Results for duplicates (repeatability)
- Performance data in standard methods (repeatability and reproducibility)
- Precision in proficiency testing schemes (reproducibility)

Bias:

- Data at many concentration levels rarely available

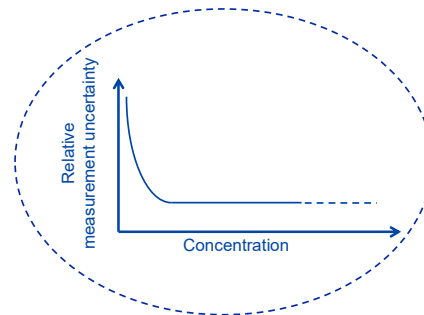
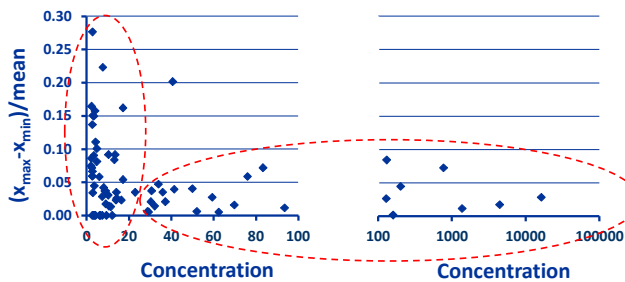
Eurachem workshop 2022

6

6

RI SE

Way of studying dependence of concentration on measurement uncertainty
Results for duplicates (repeatability)



Absolute uncertainty

Relative uncertainty

Determination of ammonium-nitrogen (EN ISO 11732). Data from Nordtest NT TR 537 (ed. 4, 2017).

Eurachem workshop 2022



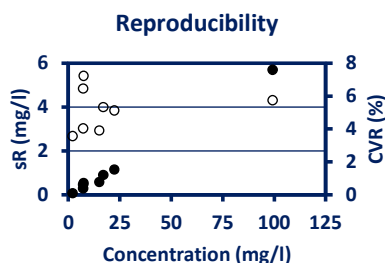
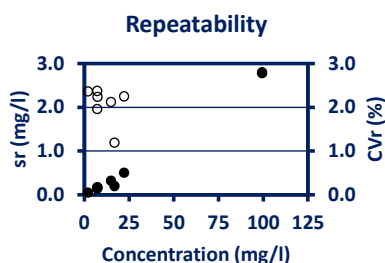
7

7

Way of studying dependence of concentration on measurement uncertainty
Performance data in standard methods

□ In many standard methods repeatability and reproducibility are given as absolute and relative standard deviation at different concentration levels.

□ Examples



● sr (left scale) ○ CVr (right scale)

● sR (left scale) ○ CVR (right scale)

Eurachem workshop 2022



8

8

Way of studying dependence of concentration on measurement uncertainty *Precision in proficiency testing schemes (reproducibility)*

From participation in proficiency test schemes covering different concentrations reproducibility expressed as absolute and relative standard deviation can give information of the concentration dependence.

Eurachem workshop 2022



9

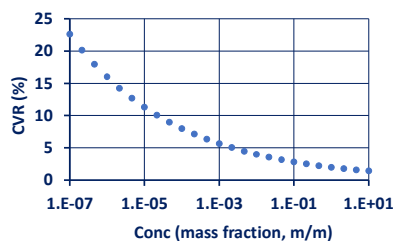
9

More on concentration dependence - Horwitz trumpet

For interlaboratory collaborative studies in food analysis:

$$s_R = 0.02 \times c^{0.85} \quad \text{or} \quad CV(\%) = 2 \times c^{-0.15}$$

where s_R is the reproducibility, $CV(\%)$ is the coefficient of variation in %, and c is concentration as mass fraction (m/m)



Note: This relationship is for large concentration ranges, and includes variation between different methods and instrumental techniques used at different concentration levels.

Eurachem workshop 2022



10

10

Uncertainty expressed as coverage interval

When expressing uncertainty as a coverage interval and

- the relative uncertainty is approx. independent of the concentration
- the (combined) standard uncertainty is > approx. 15-20 %

it is necessary to consider asymmetry in the uncertainty coverage interval

The best way of handling this is under discussion.

Eurachem workshop 2022



11

11

The end!

Thank you for listening

Eurachem workshop 2022



12

12